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Leptogenesis motivation

Two fundamental questions beyond the Standard Model



+ a series of numerical coincidences which makes it particularly effective

The 3 seesaw models



Minkowski; Gellman, Ramon, Slansky; Yanagida;Glashow; Mohapatra, Senjanovic

Scalar triplet: (type-II seesaw) $\Delta \equiv (\Delta^{++}, \Delta^{+}, \Delta^{0})$ $\mathcal{L} \ni -Y_{\Delta} \Delta L_i L_i$ $-\mu_{\Lambda}\Delta HH + h.c.$ $= Y_{\Delta} \frac{\mu_{\Delta}}{M^2} v^2$ $m_{
u}$

Magg, Wetterich; Lazarides, Shafi; Mohapatra, Senjanovic; Schechter, Valle

Fermion triplets: (type-III seesaw) $\Sigma_{i} \equiv (\Sigma_{i}^{+}, \Sigma_{i}^{0}, \Sigma_{i}^{-})$ $\mathcal{L} \ni -Y_{\Sigma_{ij}} \overline{\Sigma}_{i} L_{j} H$ $-\frac{m_{\Sigma_{i}}}{2} \overline{\Sigma}_{i}^{c} \Sigma_{i} + h.c.$



Foot, Lew, He, Joshi; Ma; Ma, Roy;T.H., Lin, Notari, Papucci, Strumia; Bajc, Nemevsek, Senjanovic; Dorsner, Fileviez-Perez;....

for example with $Y_N \sim 1$, $m_{\nu} \sim 0.1 \text{ eV}$ requires $M_N \sim 10^{15} \text{ GeV}$ with $Y_N \sim 10^{-6}$, $m_{\nu} \sim 0.1 \text{ eV}$ requires $M_N \sim \text{TeV}$

The 3 leptogenesis ingredients

first in type-l

• I) The CP-asymmetry

At $T \sim m_N$: many N in Universe thermal bath (N in thermal equilibrium) At $T \leq m_N$: the N disappear from Universe thermal bath by decaying to l + H and $\bar{l} + H^*$



The 3 leptogenesis ingredients

•2) The efficiency $\eta : \frac{n_L}{s} = \varepsilon_{N_i} \cdot \frac{n_{N_i}}{s} \Big|_{T >> M_{N_i}} \cdot \frac{\eta}{T}$ $\eta \simeq 1$: only if out-of-equilibrium: if $\Gamma_N^{Tot} \lesssim H(T = m_N)$ (+ if no fast addit. \mathbb{Z} processes) \longrightarrow if $\Gamma_N^{Tot} > H(T = m_N)$: many inverse decays \checkmark if more l than \overline{l} : more $lH \to N$ than $\overline{l}H^* \to N$ $\Rightarrow L$ asymmetry reput to 0 \rightarrow can be obtained integrating the Boltzmann equations: $Y_N = n_N/s$ $Y_L = (n_l - n_{\bar{l}})/s$ $z \equiv \frac{M_N}{T}$ $\frac{\gamma_D}{H(T=M_N)} \equiv \frac{\Gamma_N^{\text{TOT}}}{H(T=M_N)} \frac{K_1(z)}{K_2(z)} n_N^{EQ}(z)$ $\frac{s}{z}\frac{dY_N}{dz} = \left(1 - \frac{Y_N}{Y_N^{EQ}}\right) \cdot \frac{\gamma_D}{H(T = M_N)}$ $\frac{s}{z}\frac{dY_L}{dz} = \varepsilon_N \cdot \left(\frac{Y_N}{Y_N^{EQ}} - 1\right) \cdot \frac{\gamma_D}{H(T = M_N)} - 2\frac{Y_L}{Y_l^{EQ}} \cdot \frac{\gamma_{\Delta L=2}}{H(T = M_N)}$ each decay produces a $\Delta L = \varepsilon_N$ each inverse decay produces a $\Delta L = -\varepsilon_N$

if more l than \overline{l} : more $l H \to N \to \overline{l} H^*$ processes than $\overline{l} H^* \to N \to l H$

The 3 leptogenesis ingredients

• 3) The L to B conversion from SM sphalerons:

> above the EW scale B+L violating but B-L conserving SM sphalerons are in thermal equilibrium

 $T_{Decoupl.}^{Sphal.} \sim 140 \,\mathrm{GeV}$

 \Rightarrow put B+L to ~ 0 but conserving B-L:

$$\begin{array}{ccc} (B+L)_{Fin} &\sim & 0\\ (B-L)_{Fin} &= & (B-L)_{In}\\ B_{In} &= & 0 \end{array} \end{array} \xrightarrow{} B_{Fin} \sim -L_{Fin} \sim -\frac{L_{In}}{2} \\ & & \downarrow \end{array}$$
$$\begin{array}{ccc} \frac{n_B}{s} = -\frac{28}{79} \frac{n_L}{s} = -\frac{28}{79} \eta \epsilon_{N_i} \frac{n_{N_i}}{s} \Big|_{T>>M_{N_i}} \\ & & \downarrow \end{array} \\ \frac{n_B}{s} = (8.82 \pm 0.23) \cdot 10^{-11} \qquad \text{WMAP} \\ \text{Planck} \end{array}$$

Two intriguing numerical coincidences

The seesaw state mass (slight) coincidence:

• for a hierarchical spectrum of N_i : $\varepsilon_{N_1} \leq M_{N_1} \frac{3}{8\pi} \frac{1}{v^2} \sqrt{\Delta m_{atm}^2}$ $M_{N_1} << M_{N_{2,3}}$, Davidson, Ibarra '02, $M_{N_1} \gtrsim 4 \cdot 10^8 \,\mathrm{GeV}$

this scale is determined by the totally independent value of n_B/s , fits well with seesaw expectations



a much larger value of n_B/s and/or much smaller neutrino mass scale would fit much less

• for a quasi-degenerate spectrum of N_i instead: resonance occurs: ε_{N_1} not bounded

 $M_{N_1} \sim M_{N_2}$

by value of M_{N_1} or m_{ν}

 $\longrightarrow M_{N_1}$ bounded from below only by sphaleron decoupling scale

 $\longrightarrow M_{N_1} \sim \text{TeV}$ perfectly possible

Pilaftsis '97; '99; TH '02, Pilaftsis, Underwood '05; ...; Dev, Millington, Pilaftsis, Teresi '14

Two intriguing numerical coincidences

• The neutrino mass scale value versus electroweak and Planck scales coincidence

$$\longrightarrow$$
 in full generality: $\Gamma_{N_1}/H(T = M_{N_1}) \ge m_{\nu}^{Min}/10^{-3} \,\mathrm{eV}$



→ given the $m_{\nu}^{Min} < 2.2 \,\text{eV}$ direct bound or the $m_{\nu}^{Min} \lesssim 0.2 \,\text{eV}$ cosmology bound the washout from inverse decays is naturally limited ← $\Gamma_{N_1}/H(T = M_{N_1}) \leq 1$ is not much violated

real coincidence because $10^{-3} \,\mathrm{eV}$ scale is determined by independent e-w scale and Planck scale

 $10^{-3} \,\mathrm{eV} \simeq 17 \cdot 8\pi \cdot v^2 / M_{Planck}$

for example $m_{
m
u} \sim {
m KeV}$ would have given quite large washout

N.B.: no much relevant at all upper bound on $m_{
u}$ from successful leptogenesis condition

→ Buchmuller, Di Bari, Plumacher '02,'03

Abada, Davidson, Josse-Michaux, Losada, Riotto '06

TH, Lin, Notari, Papucci, Strumia '04

Flavor effects in leptogenesis

so far all results were obtained by just counting the number of lepton created and destroyed independently of whether the lepton is of e, μ or τ type a single Boltzmann equation for total lepton number

justified for $T \gtrsim 10^{12} \,\text{GeV}$: e^-, μ^-, τ^- indistinguishable in the thermal bath

same gauge interactions SM charged Yukawa interactions out of equil.

 \Rightarrow the N_1 which couples to a single $\tilde{l} \propto Y_{N_{1e}}e + Y_{N_{1\mu}}\mu + Y_{N_{1\tau}}\tau$ flavour combination creates leptons in this combination which remains coherent afterwards

 \Rightarrow one has just to count the number of l created and destroyed \Rightarrow

a single Boltzmann equation!

Flavor leptogenesis: flavor discrimination by thermal bath

However: for $T \leq 10^{12} \text{ GeV}$: $\Gamma_{\tau}^{SM} > H$ \leftarrow SM τ Yukawa interaction enters into thermal equilibr.

 \implies if $\Gamma_{\tau}^{SM} > \Gamma_{N-decay}$, SM T Yukawa interactions do occur

Abada, Davidson, Josse-Michaux, Losada, Riotto '06 Nardi, Nir, Roulet, Racker '06 Abada et al. '06; Blanchet, Di Bari, Raffelt '06 De Simone, Riotto '06, the thermal bath distinguishes τ flavor from $e + \mu$ flavor 2 Boltzmann equat.: one for number of τ and one for number of e and μ each one with its flavour asym. $\varepsilon_{N_{\alpha}} \equiv \frac{\Gamma(N \to L_{\alpha}H) - \Gamma(N \to \bar{L}_{\alpha}\bar{H})}{\Gamma_{N}^{Tot}}$ $\alpha = \tau, e + \mu$

Similarly for $T \lesssim 10^9 \,\text{GeV}$: $\Gamma^{SM}_{\mu} > H \implies \dots$ 3 Boltzmann equations, for τ , for μ and for e

(i.e. via its τ component the $\tilde{l} \propto Y_{N_{1e}}e + Y_{N_{1\mu}}\mu + Y_{N_{1\tau}}\tau$ can undergo a SM Yukawa interaction: breaks the coherence of \tilde{l} state, but this is really effective only once N inverse decay rate becomes slower than τ Yukawa rate, so that decoherence has time to occur before an inverse decay occurs)

Flavor leptogenesis typical effects

• Flavor hierarchy effect: example: if N decays much faster than H: $\frac{\Gamma_N}{H(T=m_N)} >> 1$

- in one flavor approx.: strong washout
- Barbieri, Creminelli, Strumia, Tetradis '99; Pilaftsis '05,;Pilaftsis, Underwood '05; Abada, Davidson, Josse-Michaux, Riotto '06; Nardi, Nir, Roulet, Racker '06 Abada et al. '06; Blanchet Di Bari, Raffelt '06 Pascoli, Petcov, Riotto '07; Aristizabal, Munoz, Nardi '09; Garbrecht et al '09,'11
- in two flavor case: possibility of less washout

e.g. if $\Gamma(N \to L_{e+\mu}H) >> \Gamma(N \to L_{\tau}H)$ the Y_{τ} asymmetry is not washed out even if $\frac{\Gamma_N}{H(T=m_N)} >> 1$

⇒ large flavor effects if strong washout regime $\frac{\Gamma_N}{H(T=m_N)} >> 1$ → as a result essentially no effect on $M_{N_1} \gtrsim 4 \cdot 10^8 \,\text{GeV}$ bound

• " $N_{2,3}$ -leptogenesis": in one flavor approxim. leptogenesis dominated by N_1 decays

Vives '05; Engelhard, Grossman, Nardi, Nir '06; Blanchet, Di Bari '08 \frown L asym. created by $N_{2,3}$ washed-out by N_1 Yukawa interactions

not true anymore with flavor if the N'_is mostly couple to different flavors

- Initial condition dependence: in one flavor approx. any preexisting L asym would be very easily erased by N'_is Yukawa interactions, not true anymore with flavor \Rightarrow initial cond. dependence! Bertuzzo, Di Bari, Marzola '11
 - CP-violating phase dependence: in one flavor approx. only 3 high-energy seesaw phases count with flavor: extra dependence on 3 low energy seesaw phases

 \smile including δ_{PMNS} measurable in ν -oscillations

Flavor Leptogenesis: new flavor breaking L conserving CP asymmetries

L conserving (pure flavor) asymmetries



"Purely flavored leptogenesis"

(not so easy to cook in type-I but possible)

Aristizabal Sierra, Losada, Nardi '08 Aristizabal Sierra, Munoz, Nardi '09 Gonzalez-Garcia, Racker,Rius '09

A series of additional ingredients



takes into account memory effects, off-shell effects, finite density effects, flavor oscillations, decoherence

Bhupal Dev, Millington, Pilaftsis, Teresi '14, '15

An alternative scenario: leptogenesis from N oscillations

Akhmedov, Rubakov, Smirnov '98

I) Creation of right-handed neutrinos after inflation:

→ 3 step scenario:

2)

$$n_{N_{A}} = n_{\bar{N}_{A}}, n_{N_{B}} = n_{\bar{N}_{B}}, n_{N_{C}} = n_{\bar{N}_{C}},$$

$$\downarrow$$

$$no \ L \text{ asymmetry at this stage}$$

$$M \text{ oscillations: } N_{A} \leftrightarrow N_{B}, N_{A} \leftrightarrow N_{C}, N_{B} \leftrightarrow N_{C},$$

$$\bar{N}_{A} \leftrightarrow \bar{N}_{B}, \bar{N}_{A} \leftrightarrow \bar{N}_{C}, \bar{N}_{B} \leftrightarrow \bar{N}_{C},$$

$$\bar{N}_{A} \leftrightarrow \bar{N}_{B}, \bar{N}_{A} \leftrightarrow \bar{N}_{C}, \bar{N}_{B} \leftrightarrow \bar{N}_{C},$$

$$\bar{N}_{A} \leftrightarrow \bar{N}_{B}, \bar{N}_{A} \leftrightarrow \bar{N}_{C}, \bar{N}_{B} \leftrightarrow \bar{N}_{C},$$

$$CP \text{-violation in } M_{N_{ab}}$$

$$n_{N_{A}} \neq n_{\bar{N}_{A}}, n_{N_{B}} \neq n_{\bar{N}_{B}}, n_{N_{C}} \neq n_{\bar{N}_{C}},$$
but still with L conserved:
$$n_{N_{A}} + n_{N_{B}} + n_{N_{C}} = n_{\bar{N}_{A}} + n_{\bar{N}_{B}} + n_{\bar{N}_{C}}$$

An alternative scenario: leptogenesis from N oscillations

Akhmedov, Rubakov, Smirnov '98

3) Assume: - on the one hand: $Y_{N_{A,B}}$ large enough for $\Gamma_{N_{A,B}}^{Yuk.} > H$ before sphaleron decoupling: $T_{sphaleron} \simeq 140 \text{ GeV}$

- on the other hand: Y_{N_C} small enough for $\Gamma_{N_C}^{Yuk.} < H$ before sphaleron decoupling:

 \Rightarrow final net baryon asymmetry

An alternative scenario: leptogenesis from N oscillations

In practice: requires: • N masses small: $1 \text{ GeV} \lesssim m_{N_{A,B,C}} \lesssim 100 \text{ GeV}$

to avoid N's are to avoid too fast

decaying during BBN $N_i \leftrightarrow \bar{N}_i$ processes putting $n_{N_i} - n_{\bar{N}_i}$ asym. to 0

• Yukawa couplings in agreement with neutrino mass constraints

R

 \Rightarrow recently reconsidered in details with flavor effects included,.... Drewes, Garbrecht '13 ← works well in multi GeV range

Scenarios without L violation in CP asymmetries



$$\begin{array}{cccc} n_{l_{L}} \neq n_{\overline{l_{L}}}, & n_{l_{R}} \neq n_{\overline{l_{R}}} \\ \text{sphalerons} & \downarrow & & \\ n_{b} - n_{\overline{b}} & n_{b} - n_{\overline{b}} \end{array} & \begin{array}{c} n_{l_{L}} + n_{l_{R}} = n_{\overline{l_{L}}} + n_{\overline{l}} \\ \text{L-violation from sphalerons} \\ \text{net B asymmetry} \end{array}$$

Type-III leptogenesis: decays of fermion triplets: $\Sigma_i \equiv (\Sigma_i^+, \Sigma_i^0, \Sigma_i^-)$

 ν_{Li}

h

 Σ_i^0

TH,Lin,Notari,Papucci,Strumia '03

 ν_{Lk}

h

- generation of \mathcal{V} masses unchanged: $\Sigma_i^0 \leftrightarrow N_i$
- leptogenesis diagrams involve both neutral and charged seesaw states:



Type-III seesaw bounds





PS: flavor effects work the same way as in type-I except that when $\gamma_A > \gamma_D$ they are totally irrelevant (gauge scattering are flavor blind) Aristizabal, Kamenek, N

Aristizabal, Kamenek, Nemvesek, '10 TH '12



Type-II leptogenesis: decays of a scalar triplet: $\Delta_L = (\Delta_L^{++}, \Delta_L^+, \Delta_L^0)$

TH, Raidal, Strumia '06

 \Rightarrow doesn't change the typical leptogenesis scale:

Hierarchical mass spectrum: $m_{\Delta_{L1}} \ll m_{\Delta_{L2}}, m_{N_i}$: $m_{\Delta} > 3 \cdot 10^{10} \,\text{GeV}$

Quasi-degenerate mass spectrum: $m_{\Delta_{L1}} \sim m_{\Delta_{L2}}$: $m_{\Delta} > 1.6 \,\mathrm{TeV}$

TH,Raidal,Strumia '06

 \Rightarrow but does change a lot the asym. creation dynamics!

Strumia '09

 \frown creation of a $\Delta-ar{\Delta}$ asym. first, reprocessed in a L asym. later on

 \checkmark allows to avoid any efficiency suppression: if $Br(\Delta_L \to LL) >> Br(\Delta_L \to HH)$

Type-II leptogenesis: flavor effects

⇒ Purely Flavoured Leptogenesis generically dominant for a very large part of parameter space

Flavor effects are always present for type-II leptogenesis

Type-I+ Type-II: contribution of Δ_L to N CP-asymmetry

L-R and SO(10) models

• if $M_N << m_\Delta$ the N decays dominate naturally leptogenesis but still there is a triplet contribution to the CP-asymmetry

can easily be dominant (e.g. if $\mathcal{m}_{
u}$ dominated by type-II contribution) and lead to successful leptogenesis

see also Antusch, King '04

What about SUSY for leptogenesis

 \rightarrow SUSY seesaw leptogenesis works the same way as non-SUSY case up to factors of O(1)

→ in addition it allows new scenarios: ''Soft leptogenesis''

right-handed sneutrinos soft terms bring new source of L violation and CP violation Boubekeur '02; D'Ambrosio, Giudice, Raidal '03; Grossman, Kashti, Nir, Roulet '03;

$$\mathcal{L}_{soft} \ni (-AY_{N_{i\alpha}}\tilde{N}_{i}\tilde{l}_{\alpha}H_{u} - \frac{1}{2}BM_{i}\tilde{N}_{i}\tilde{N}_{i} + h.c.) - \tilde{M}_{ij}^{2}\tilde{N}_{i}^{*}\tilde{N}_{j}$$

⇒ CP asymmetry from 1-loop self energy and vertex diagrams

D'Ambrosio, Giudice, Raidal '03; Grossman, Kashti, Nir, Roulet '03; D'Ambrosio, TH, Hektor, Rossi, Raidal '04;

can work typically within the range: $10^3 \,{\rm GeV} \lesssim m_{\tilde{N}} \lesssim 10^9 \,{\rm GeV}$

see recent review: Fong, Gonzalez-Garcia, Nardi '12

Testing low scale leptogenesis at colliders?

 \rightarrow by producing low scale seesaw states at colliders?

• type-I: very difficult:

 $Y_N \sim 10^{-6}$ for $M_N \sim 1 \,\mathrm{TeV}$

Dev, Millington, Pilaftsis, Teresi '14

 $\mu \to e\gamma$

too large for LHC

see Plumacher et al,

Frère et al, Babu et al Fileviez-Perez et al,...

 $\mu \rightarrow eee$

Yukawa couplings are expected far too small to allow $N \ {\rm production}$

in special cases larger Y_N are allowed,

 \longrightarrow allowing N production + observable charged lepton flavor violation

production mechanisms other than Yukawa

• type-II and type-III: Drell-Yan pair production mechanisms

problem: production interactions tend to thermalize the seesaw state \implies leptogenesis suppressions!

->> SM gauge interact, for type-II and III: $m_{\Delta,\Sigma} > 1.6\,{
m TeV}$

 $\longrightarrow N$ production via Z': similar bounds as for type-II/III

 \rightarrow N production via W_R : much more dramatic thermalization effect!

involves only one heavy external state instead of two \Rightarrow only one Boltzm. suppression power instead of 2 scattering is never slower than the decay $\Rightarrow m_{W_R} \gtrsim 18 \text{ TeV}$

Dev, Lee, Mohapatra '14, '15

High scale leptogenesis tests?

in SUSY neutrino mass matrix knowledge and rare lepton flavour violating processes allows to reconstruct in principle the full seesaw lagrangian
 Davidson, Ibarra '03 the model can be overconstrained by the baryon asymmetry constraint but basically impossible to do in practice and based on the difficult to test assumption of universality of soft terms

in specific GUT models one can have a closer relation between neutrino data and leptogenesis: we miss a successful example of one-to-one correspondance

> e.g. normalization factors as overall seesaw scale are left free and leptogenesis crucially depends on them

> > see for example Frigerio, Hosteins, Lavignac, Romanino '08

>> or as well known if neutrinos are proven to have inverted hierarchy or quasi-degenerate with no corresponding $0\nu 2\beta$ signal, usual seesaw falsified

Leptogenesis at TeV scale with non seesaw neutrino mass sources

> several mechanisms: - resonance

- hierarchy of L -violating couplings with radiative neutrino masses TH '02

TH '02

- 3-body decays with radiative neutrino masses тн '02
- radiative seesaw neutrino masses Ma '07; TH, Ling, Lopez-Honorez, Rocher '08; Gu, Sarkar '08

 \Rightarrow many possibilities: $-N_i + S^+$: - 3-body decays

-

....

- soft leptogenesis: - resonance

- hierarchy of couplings

Frigerio, TH, Ma '02

- 4th generation of leptons: hierarchy of couplings Abada, Losada '03

Boubekeur '02; Giudice et al. '03; Grossman et al '04; TH, March-Russel, West '04

- hierarchy of couplings with radiative $m_{
u}$ Boubekeur, TH, Senjanovic '04

- ε' type CP-violation Grossman, Kashti, Nir, Roulet '04

- N_i + Dark Matter inert Higgs doublet: hierarchical couplings

Ma '07;TH, Ling, Lopez-Honorez, Rocher '08; Gu, Sarkar '08

- scalar singlet + scalar triplet Gu, He, Sarkar, Zhang '09
- scalar singlet + extra fermion triplet Patra '09
- N_i + various scalars Fong, Gonzalez-Garcia, Nardi, Peinado '13

Some of these models are testable to a large extend at the price of giving up the seesaw and/or adding new fields

Despite of the fact that to test leptogenesis remains a really tough problem, even more difficult than to test the seesaw, leptogenesis remains very well motivated and the most straightforward explanation we have for the baryon asymmetry of the Universe

could have been very well realized in Nature!

Flavour leptogenesis: spectator process effects

Given the neutrino data: no relevant bound on m_{ν} from leptogenesis

Flavour leptogenesis: mass bounds with flavour

• the $M_{N_1}\gtrsim 4\cdot 10^8\,{
m GeV}\,$ bound essentially unaffected $\,$ set

see Antusch, Blanchet, Blennow, Fermandez-Martinez '10 Racker, Pena, Rius '12

• the $m_{\nu} \lesssim 0.12 \,\text{eV}$ one-flavor bound for N_i hierarchical spectrum can be largely relaxed (but was for an unlikely situation anyway)

Riotto et al. '06

Flavour leptogenesis: effect of low energy PMNS phase

effect of low energy phases: in one flavor approx. leptogenesis depends only on the 3 high energy phases

with several flavours it depends in addition on the 3 low energy phases (in PMNS matrix)

Pascoli, Petcov, Riotto '06

with flavour the PMNS Dirac phase alone can lead to successful leptogenesis

without flavour such a non zero phase would also basically imply leptogenesis because no reason from the UV physics point of view to have only the low-energy phases: UV doesn't care about low energy phenomenological phase values

Flavour leptogenesis: N₂ leptogenesis

Vives '05; Engelhard, Grossman, Nardi, Nir '06; Blanchet, Di Bari '08

" N_2 leptogenesis": in one flavour approx: asym. created by $N_{2,3}$ very easily washed out by N_1

hot true anymore with several flavours for special cases with different flavour hierarchies between various N_i

interesting for SO(10) models which in simplest version give

 $m_{N_1} << m_{N_2} << m_{N_3} \implies m_{N_1} < 10^8 \,\mathrm{GeV}$

Gauge scattering thermalization effect

 $\Delta \bar{\Delta} \leftrightarrow W^+ W^-, ZZ, f\bar{f}, \dots$ $\Sigma \bar{\Sigma} \leftrightarrow W^+ W^-, ZZ, f\bar{f}, \dots$

▶ put the ∆, ∑ into thermal equilibrium suppression effect as long as ∆, ∑ gauge scatter before it decays, i.e. as long as: $\frac{\gamma_A}{n_{\Delta,\Sigma}^{Eq}} \gtrsim \frac{\gamma_D}{n_{\Delta,\Sigma}^{Eq}}$

model and flavor independent bound on lepton asymmetry produced

TH '12

$$Y_L \lesssim \varepsilon_{\Delta,\Sigma} \int_{z_{in}}^{z_A} \frac{dY_{\Delta,\Sigma}^{Eq}}{dz} \frac{\gamma_D}{4\gamma_A} dz + \varepsilon_{\Delta,\Sigma} Y_{\Delta,\Sigma}^{Eq} \simeq \varepsilon_{\Delta,\Sigma} Y_{\Delta,\Sigma}^{Eq}(z_A) \left(z_A/4 + 1 \right)$$