

EDMs: particle physics for the poor

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“Beyond the Standard Model with neutrinos & nuclear physics”

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With Jordy de Vries, Emanuele Mereghetti, Cheng-Pang Liu, Bira van Kolck



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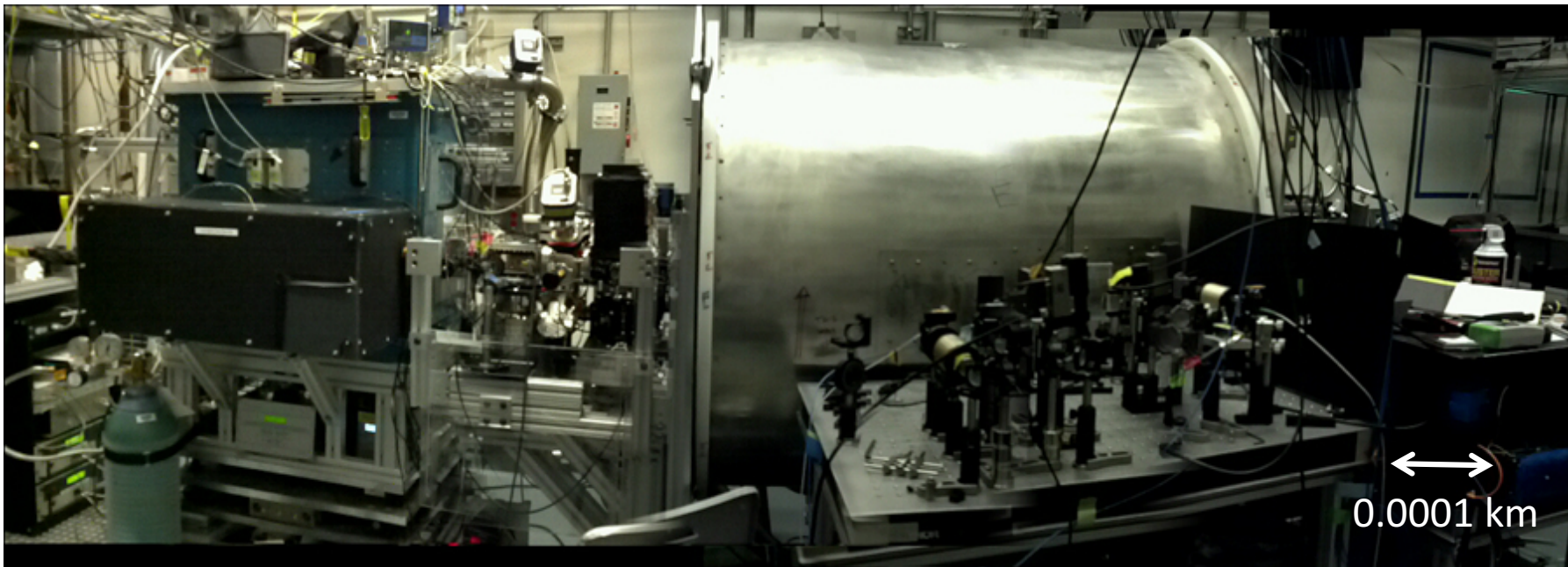
A new world record

- ✓ J. Baron *et al.* (Harvard-Yale)
 - Science **343**, 269 (2014)
 - New J. Phys. **19**, 073029 (2017)

Order of Magnitude Smaller Limit on the Electric Dipole Moment of the Electron

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The Standard Model of particle physics is known to be incomplete. Extensions to the Standard Model, such as weak-scale supersymmetry, posit the existence of new particles and interactions that are asymmetric under time reversal (T) and nearly always predict a small yet potentially measurable electron electric dipole moment (EDM), d_e , in the range of 10^{-27} to 10^{-30} e·cm. The EDM is an asymmetric charge distribution along the electron spin (S) that is also asymmetric under T. Using the polar molecule thorium monoxide, we measured $d_e = (-2.1 \pm 3.7_{\text{stat}} \pm 2.5_{\text{sys}}) \times 10^{-29}$ e·cm. This corresponds to an upper limit of $|d_e| < 8.7 \times 10^{-29}$ e·cm with 90% confidence, an order of magnitude improvement in sensitivity relative to the previous best limit. Our result constrains T-violating physics at the TeV energy scale.



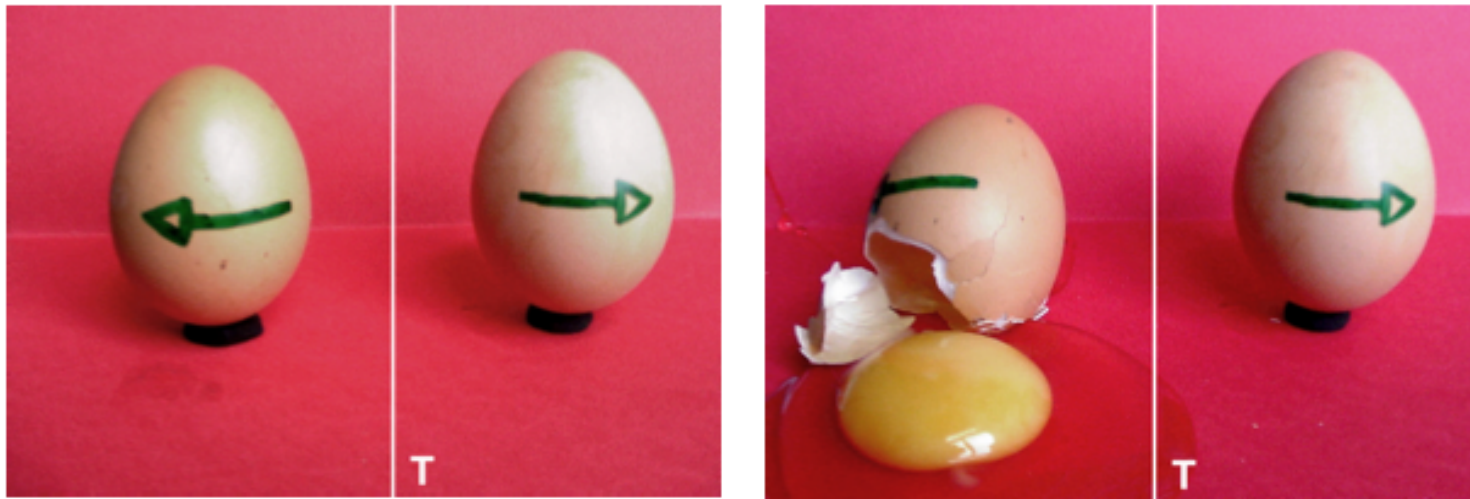
Game plan

1. Towards discovery
 - ✓ EDMs in the SM and beyond
 - ✓ The classic experiments
2. Towards interpretation, top-down versus bottom-up
 - ✓ Unraveling microscopic T violation: EFT for EDMs
3. Hadronic EDMs
 - ✓ Nucleons, light nuclei & diamagnetic atoms
4. [... The electron EDM
 - ✓ Paramagnetic atoms & molecules...]
5. Take-home messages



What is an EDM?

- ✓ A permanent EDM violates P & T, hence [CPT theorem →] also CP
 - Permanent charge separation along the spin axis, unit = “e cm”



PhD thesis
J. J. Hudson

- ✓ An atomic physics quantity of interest to particle physics

$$\mathcal{L} = \frac{d}{2} \bar{\psi} \gamma_5 \sigma_{\mu\nu} \psi F^{\mu\nu} \rightarrow H = -d \vec{\sigma} \cdot \vec{E}$$

- EDM = “dimension-6 operator”
- SM EDMs are inaccessible, but expected just “beyond” SM

The hunt for discovery

	System	Group	Limit in $e\text{ cm}$	C.L.	Value in $e\text{ cm}$	Year
electron	^{205}Tl	Berkeley	1.6×10^{-27}	90%	$6.9(7.4) \times 10^{-28}$	2002
	YbF	Imperial	10.5×10^{-28}	90	$-2.4(5.7)(1.5) \times 10^{-28}$	2011
	$\text{Eu}_{0.5}\text{Ba}_{0.5}\text{TiO}_3$	Yale	6.05×10^{-25}	90	$-1.07(3.06)(1.74) \times 10^{-25}$	2012
	PbO	Yale	1.7×10^{-26}	90	$-4.4(9.5)(1.8) \times 10^{-27}$	2013
	HfF ⁺	JILA/Boulder	1.3×10^{-28}	90	$0.9(7.7)(1.7) \times 10^{-29}$	2017
	ThO	Harvard/Yale	9.4×10^{-29}	90	$-2.2(4.8) \times 10^{-29}$	2014
	muon	E821 BNL $g-2$	1.8×10^{-19}	95	$0.0(0.2)(0.9) \times 10^{-19}$	2009
	neutron	Sussex-RAL-ILL	3.0×10^{-26}	90	$-0.21(1.82) \times 10^{-26}$	2015
	^{129}Xe	UMich	6.6×10^{-27}	95	$0.7(3.3)(0.1) \times 10^{-27}$	2001
	^{199}Hg	UWash	7.4×10^{-30}	95	$2.20(2.75)(1.48) \times 10^{-30}$	2016
	^{225}Ra	ANL	1.4×10^{-23}	95	$4.0(6.0)(0.2) \times 10^{-24}$	2016

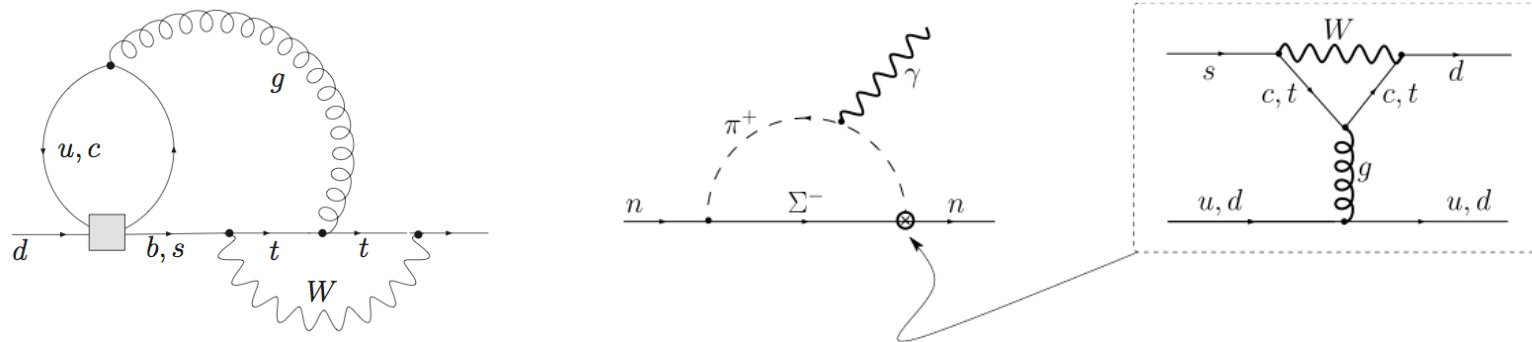
✓ 25-30 more-or-less small-scale expt's worldwide with \approx 500 researchers

Electroweak CP violation

- ✓ CKM quark-mixing matrix
 - All CP-odd effects involve 3 quark families
 - Jarlskog invariant $J_{CP} = \sin^2\theta_{12}\sin\theta_{13}\sin\theta_{23}\sin\delta_{CKM} \approx 3 \times 10^{-5}$

- ✓ EDMs due to δ_{CKM} are unmeasurably small
 - EDM = 2nd-order T-violation at least *e.g.* $(d_n)_{CKM} \approx (10^{-7})^2 J_{CP} e/M$
 - Quark EDMs = 0 at 2-loop order $\rightarrow (d_n)_{CKM} = O(10^{-32}) e \text{ cm}$
 - Electron EDM = 0 at 3-loop order $\rightarrow (d_e)_{CKM} = O(10^{-38}) e \text{ cm}$

- ✓ “Long-distance” contributions to n EDM



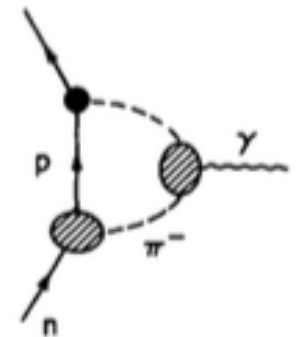
The QCD vacuum angle

- ✓ Observed symmetries *almost* perfectly match those of QCD

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4}G_{\mu\nu}^a G^{a,\mu\nu} + \bar{q}(i\not{D} - M)q - \bar{\theta} \frac{g^2}{64\pi^2} \epsilon^{\mu\nu\alpha\beta} G_{\mu\nu}^a G_{\alpha\beta}^a$$

- Total derivative, but modifies physics: P and T violation
- Strong CP problem: $d_n \rightarrow \bar{\theta} = \theta + \arg \det M_q \leq O(10^{-10})$, not $O(1)$...

- ✓ Long-distance contributions to n EDM \rightarrow non-perturbative QCD
 - “Soft-pion” theorem: Chiral log dominates $d_n \sim \theta \log m_\pi^2$
 - Nowadays: Chiral perturbation theory = EFT for QCD

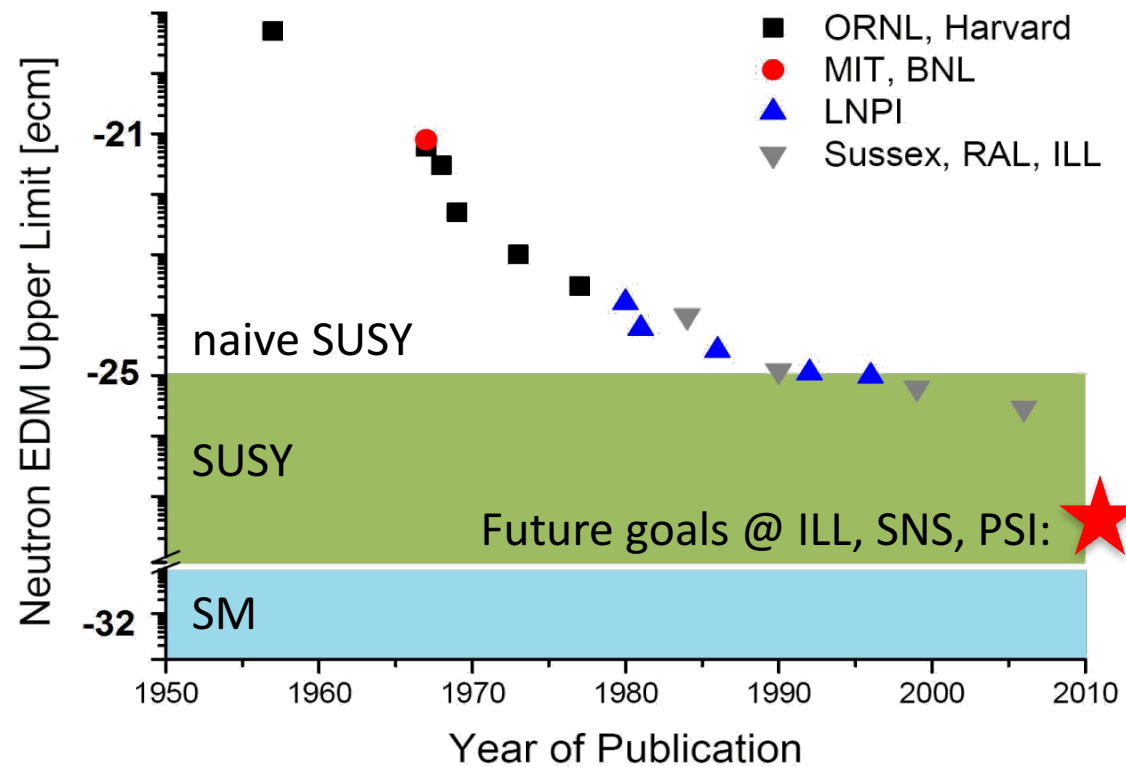


- ✓ A nonzero EDM implies new, super-weak physics
 - EDMs arise at 1-loop level from new δ_{CP} 's OR from θ_{QCD} (also new!)

Neutron EDM

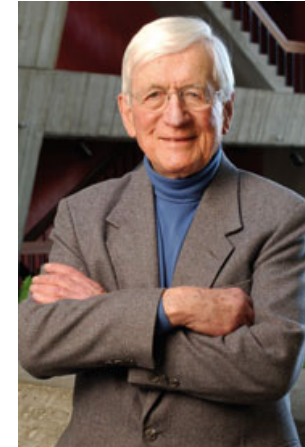
✓ Strong CP problem

– If $\theta = O(1) \rightarrow d_n = O(10^{-15}) e \text{ cm}$ would have been discovered in 1950s

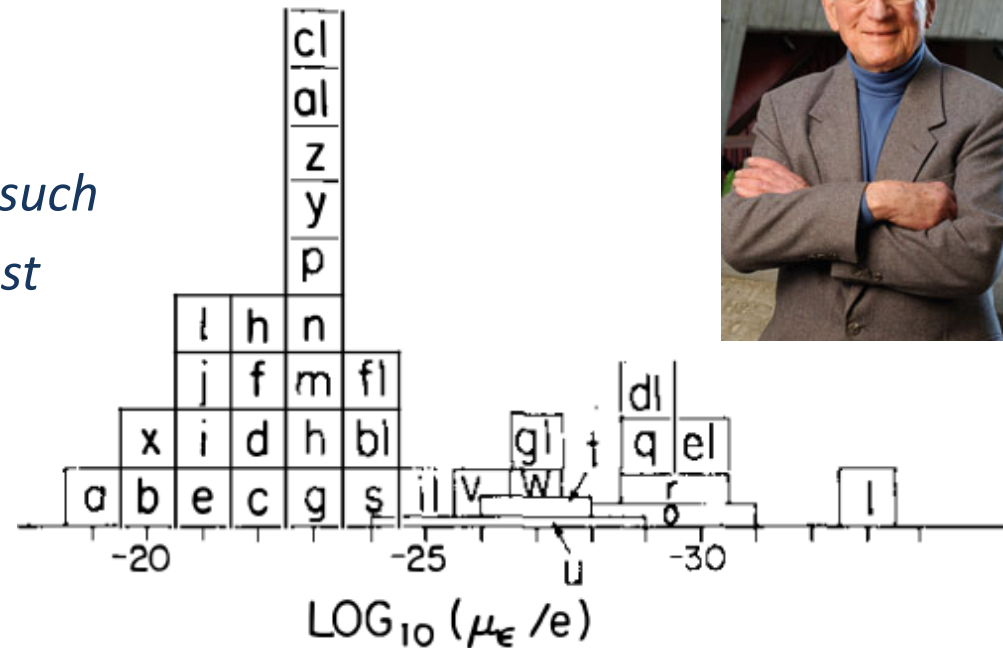


The killer n EDM

- ✓ Norman Ramsey (1915-2011)
 - “Ultimately the validity of all such symmetry arguments must rest on experiment”



- ✓ Purcell & Ramsey (1950)
 - P violation
- ✓ Lee & Yang, Landau (1957)
 - T violation
 - CP = true mirror?
 - No! (1964)
- ✓ First direct limit (1951 → 1957)
 - $d_n = -0.1(2.4) \times 10^{-20} e \text{ cm}$



a. Feinberg (1965) (EM)	u. Mohapatra & Pati (1975) (MW)
b. Salzman & Salzman (1965) (EM)	v. Clark & Randa (1975) (MS)
c. Barton & White (1969) (EM)	w. Chodos & Lane (1972) (MW)
d. Broadhurst (1970) (EM)	x. Feinberg & Mani (1965) (W, $\Delta S = 1$)
e. Babu & Suzuki (1967) (MW, $\Delta S = 0$)	y. Gourishankar (1968) (MW, $\Delta S = 1$)
f. Meister & Rhada (1964) (MW, $\Delta S = 0$)	z. Filipov et al (1968) (EM)
g. Gourishankar (1968) (MW, $\Delta S = 1$)	a1. McNamee & Pati (1969) (MW, $\Delta S = 0, 1$)
h. McNamee & Pati (1969) (MW, $\Delta S = 0, 1$)	b1. Barton & White (1969) (EM, MW, $\Delta S = 0, 1$)
i. Nishijima & Swank (1967) (MW, $\Delta S = 0$)	c1. McCliment & Teeters (1970) (MW)
j. Nishijima (1969) (MW, $\Delta S = 0$)	d1. Frenkel & Ebel (1974a,b)
k. Boulware (1965) (MW, $\Delta S = 0$)	e1. Nanopoulos & Yildiz (1979) (Q)
l. Wolfenstein (1964a,b) (SW, $\Delta S = 2$)	f1. Eichten et al (1980) (MW, H)
m. Pais & Primack (1973a,b) (MW)	g1. Ellis et al (1980, 1981) (this paper has the interesting characteristic that it establishes an order-of-magnitude lower limit to D of $3 \times 10^{-28} \text{ cm}$)
n. Lee (1973, 1974) (MW)	h1. Crewther et al (1979)
o. Okun (1969) (SW)	i1. Shizuya & Tye (1980) (MW, H)
p. Mohapatra (1972) (MW)	j1. Epstein (1980)
q. Frenkel & Ebel (1974a) (MW)	
r. Wolfenstein (1974) (SW)	
s. Weinberg (1976) (MW)	
t. Pakvasa & Tuan (1975) (MW)	

The killer eEDM

✓ 2014: new world record

✓ Paramagnetic atoms

$$- d_{\text{atom}} = K_{\text{relativistic}} \times d_e$$

✓ Polar molecules

Ion-like charge separation

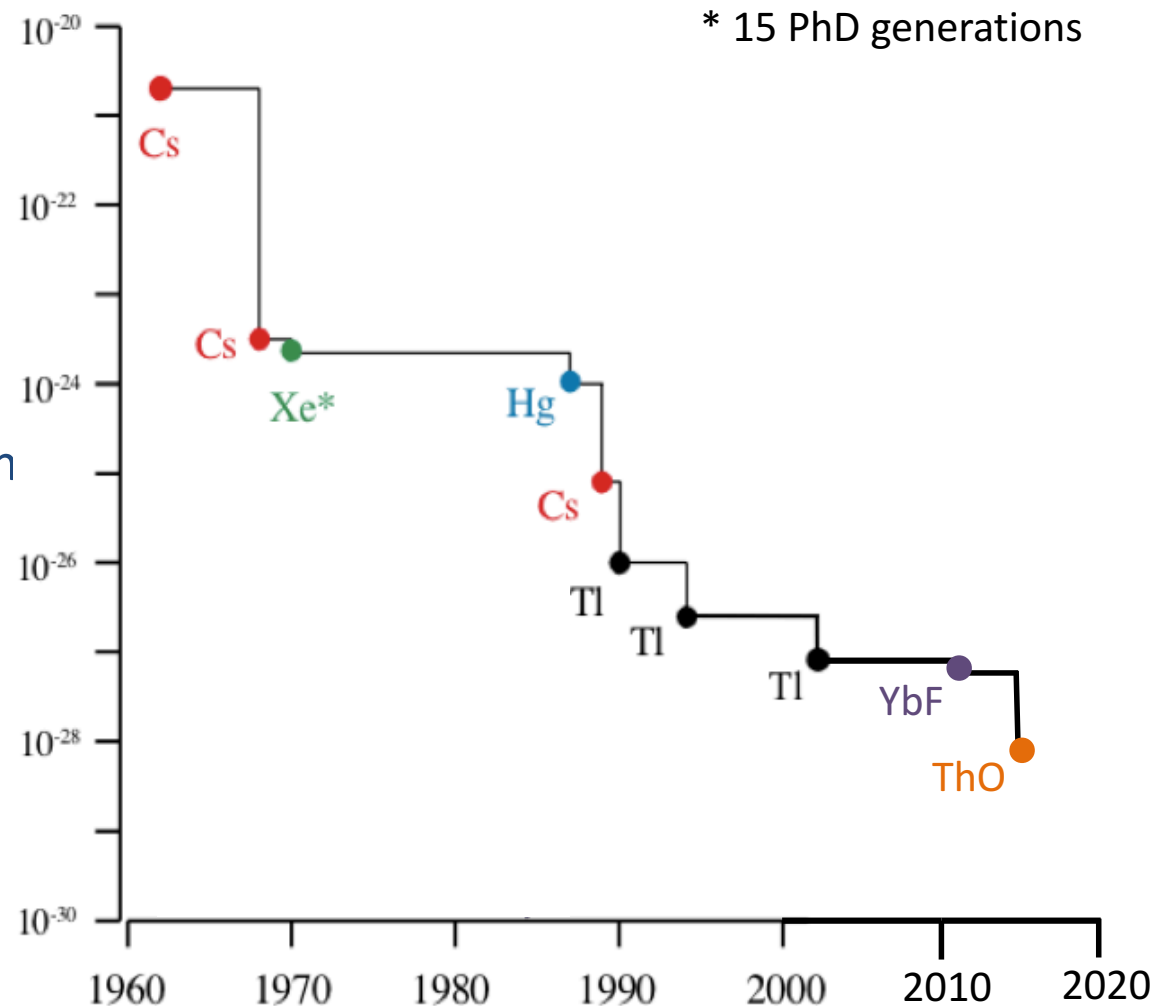
$$E_{\text{int}} \approx 75 \text{ GV/cm}$$

$$E_{\text{ext}} \approx 10\text{-}10^4 \text{ V/cm}$$

✓ SM value reached in

- 2075 for neutron*

- 2115 for electron...



✓ Upper limit $|d_e| < 8.7 \times 10^{-29} e \text{ cm}$ \rightarrow scale of new physics $\Lambda > \text{few TeV}$

The need for interpretation

- ✓ Limit on ^{199}Hg EDM
 - Swallows *et al.*, 2013
 - Lots of crappy modeling

- ✓ “Just one number?”
 - Gives *scale* of new physics

- ✓ The EDM program:
 - How to disentangle the different sources of T violation?
 - How many & which observables are needed?
 - EFT from 1st principles: systematic + model independent + errors

TABLE IV. Limits on CP -violating parameters (defined in the text) based on our new experimental limit for $d(^{199}\text{Hg})$ (95% C.L.) compared to limits from the YbF (90% C.L.) [38], Tl (90% C.L.) [37], neutron (90% C.L.) [47], or TlF (95% C.L.) [59] experiments. Values that improve upon (complement) previous limits appear above (below) the horizontal line. Particle theory interpretation references are given in the last column.

Parameter	^{199}Hg bound	Hg theory	Best other limit
$\tilde{d}_q(\text{cm})^a$	6×10^{-27}	[58]	n: 3×10^{-26} [60]
$d_p(e \text{ cm})$	8.6×10^{-25}	[46]	TlF 6×10^{-23} [61]
C_{SP}	6.6×10^{-8}	[34]	Tl 2.4×10^{-7} [62]
C_{PS}	5.2×10^{-7}	[39]	TlF 3×10^{-4} [5]
C_T	1.9×10^{-9}	[39]	TlF 4.5×10^{-7} [5]
$\bar{\theta}_{QCD}$	5.3×10^{-10}	[56]	n 2.4×10^{-10} [60]
$d_n(e \text{ cm})$	6.3×10^{-26}	[46]	n 2.9×10^{-26} [60]
$d_e(e \text{ cm})$	3×10^{-27}	[33,36]	YbF 1.05×10^{-27} [60]

^aFor ^{199}Hg , $\tilde{d}_q = (\tilde{d}_u - \tilde{d}_d)$; for n, $\tilde{d}_q = (0.5\tilde{d}_u + \tilde{d}_d)$.

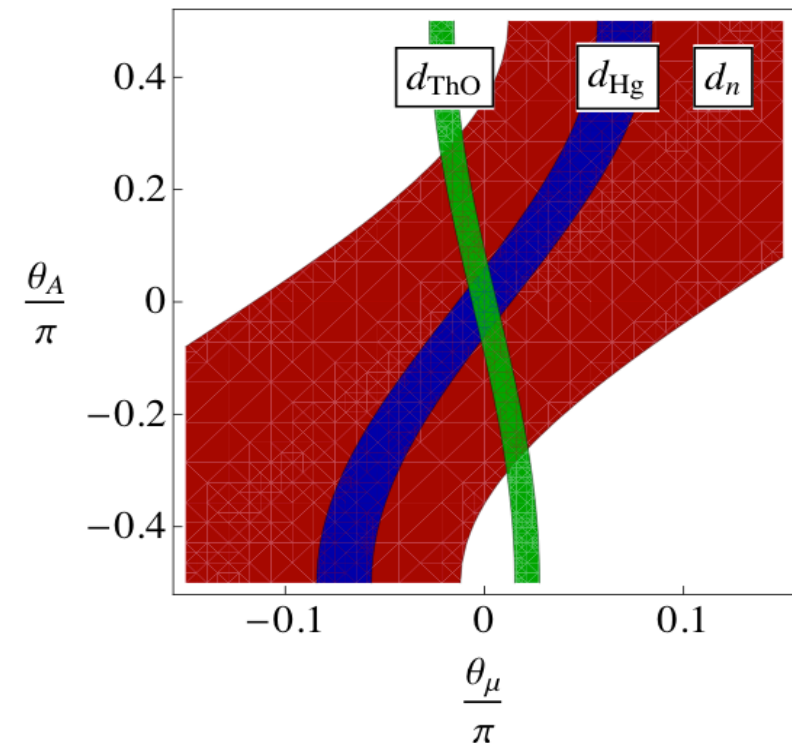
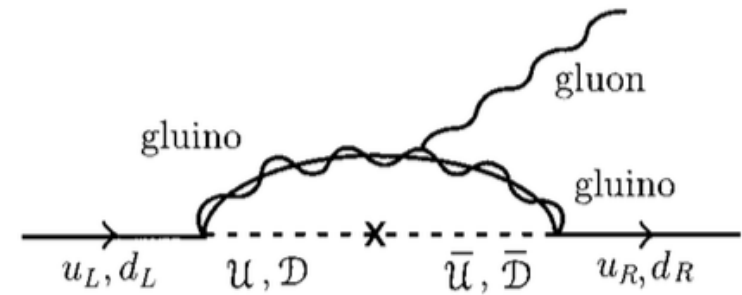
The SUSY CP problem

- ✓ MSSM has > 100 parameters, 10s δ_{CP} -like
- ✓ Typical SUSY prediction (NDA, $m_d = 7$ MeV)

$$d_n = 5 \cdot 10^{-24} \frac{\text{Im}A'_d(100 \text{ GeV})^2}{m_{\text{gluino}}^3} e \text{ cm}$$

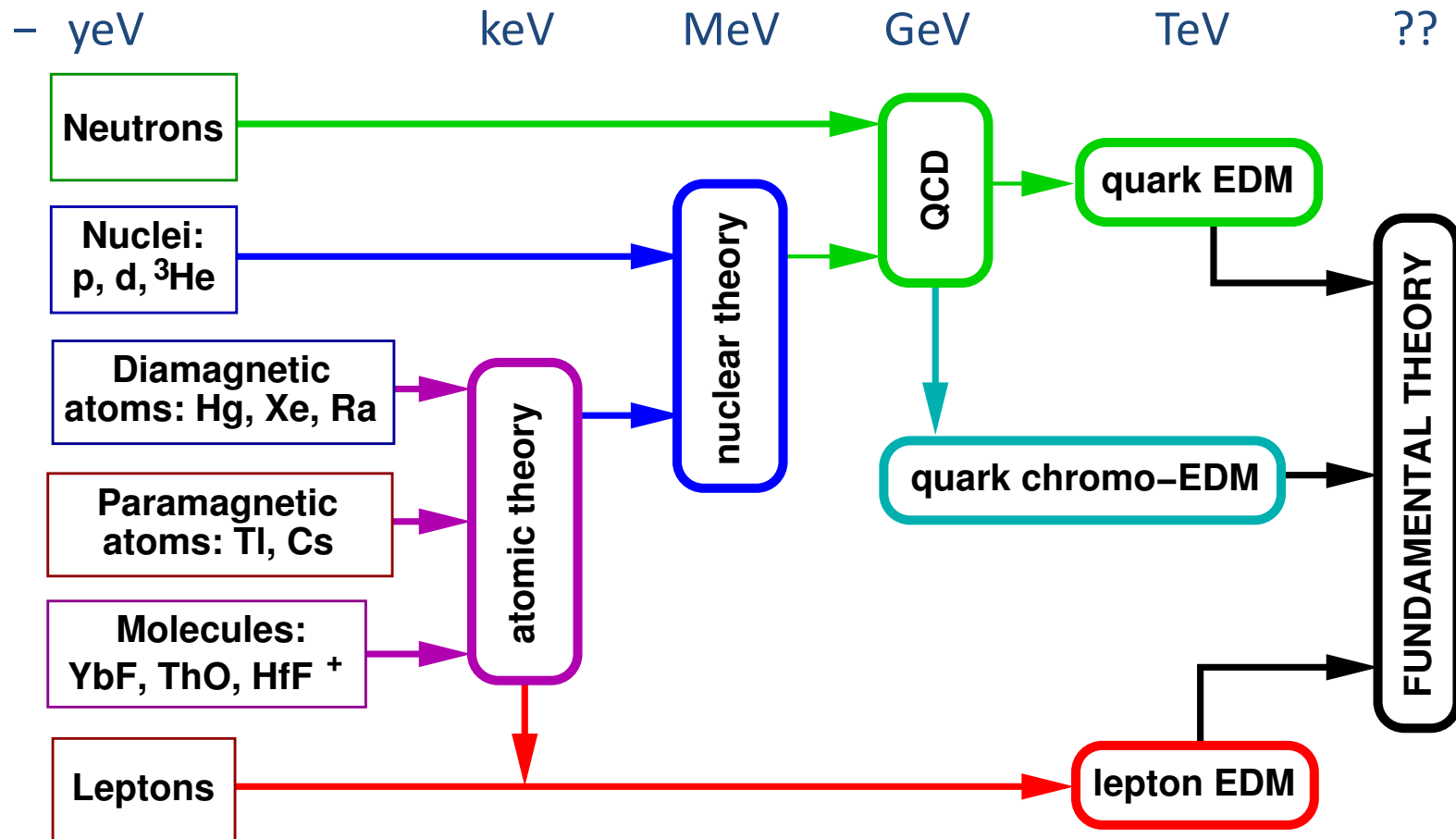
$$A'_d \sim \tan \beta = v_2/v_1$$

- ✓ eEDM & dEDM enhanced for large $\tan \beta$
 - Friction with Higgs mass?
- ✓ Unnatural SUSY scale?
 - M_{SUSY} from 500 GeV \rightarrow 2 TeV
- ✓ Current EDM null results \rightarrow probe 1-10 TeV scale or $\delta_{CP} \leq O(10^{-2})$
 - Next generation \rightarrow sensitive to 10-100 TeV scale or $\delta_{CP} \leq O(10^{-4})$



The EDM landscape

✓ Scales



✓ Theory is essential for the interpretation of EDMs of complex systems

The Standard Model as an effective field theory

- ✓ Add to the SM all possible P- and T-odd interactions

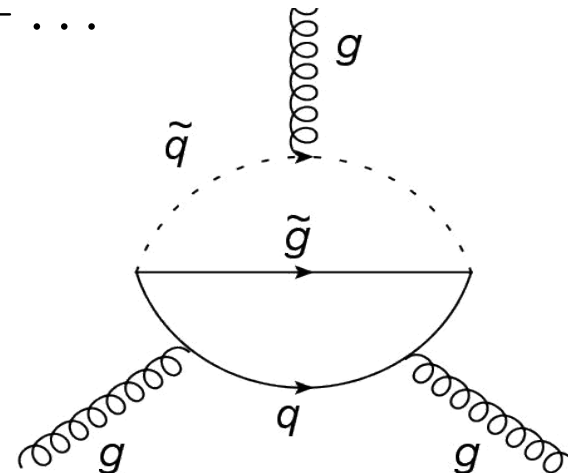
$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}^{d=5} + \frac{1}{\Lambda^2} \mathcal{L}^{d=6} + \dots$$

- ✓ Integrate out heavy (new) particles

- ✓ 1 TeV?

Q

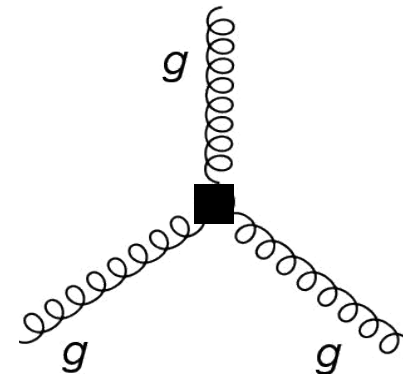
Effectively becomes $O(1/\Lambda^2)$



- ✓ 100 GeV

gluon color-EDM

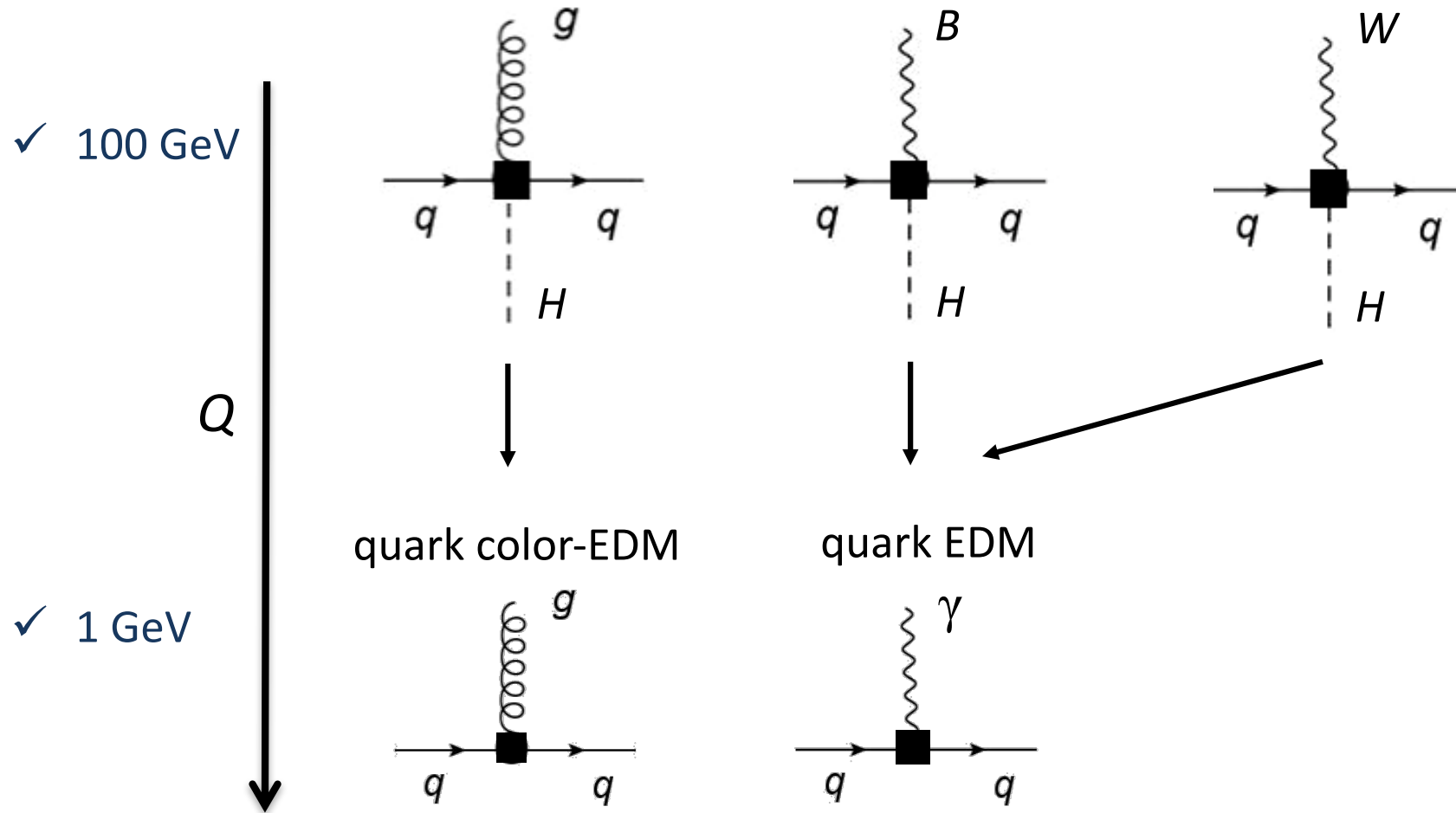
$$d_W f^{abc} \epsilon^{\mu\nu\alpha\beta} G_{\alpha\beta}^a G_{\mu\lambda}^b G_{\nu}^{c\lambda}$$



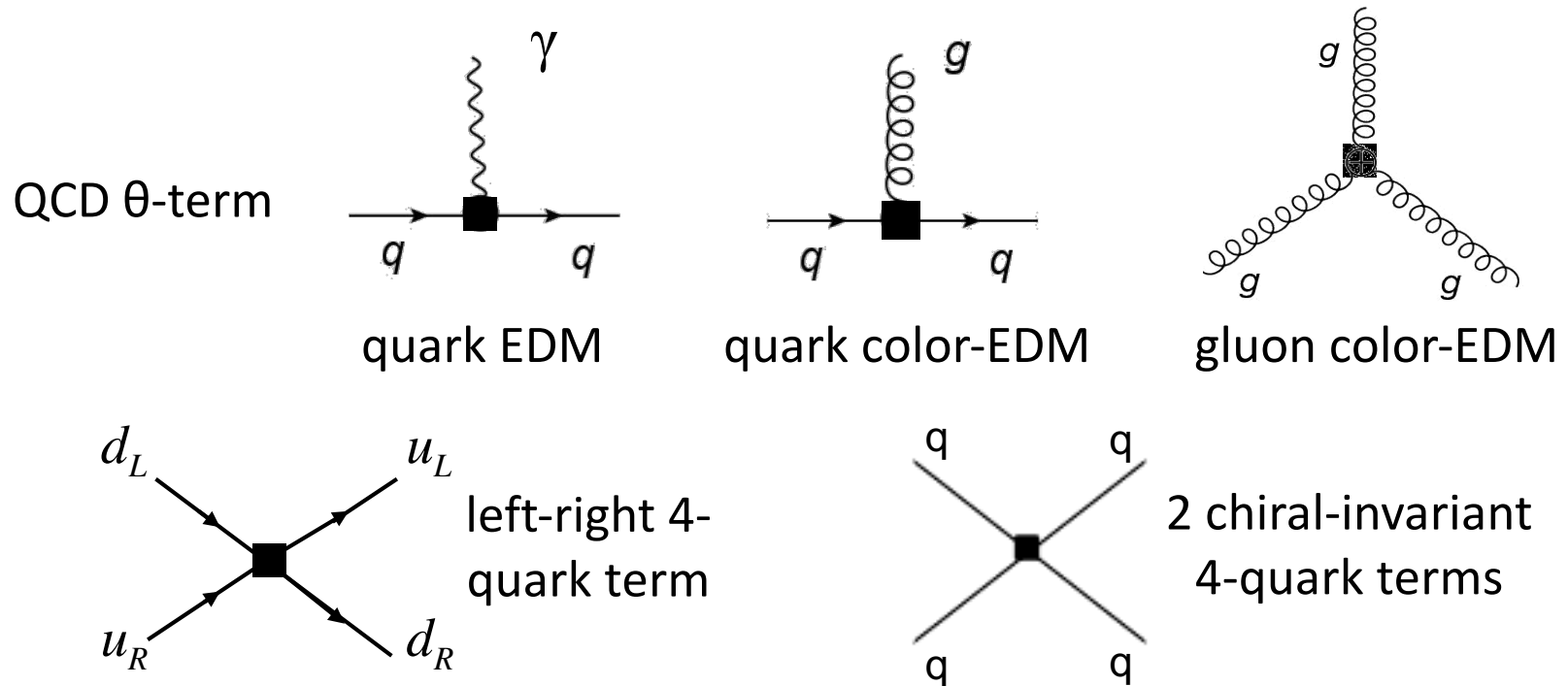
$$d_W \sim \frac{1}{\Lambda^2}$$

Dimension-6 sources

- ✓ Electroweak symmetry breaking, integrate out heavy particles
 - EDMs flip chirality → effectively dimension 6, prop. to $m = g_{\text{Yukawa}} v/\sqrt{2}$



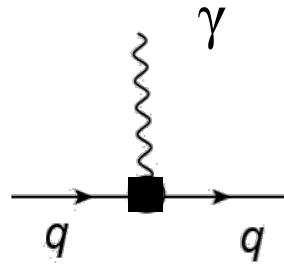
Summary: dimension-4 and -6 sources @ 1 GeV



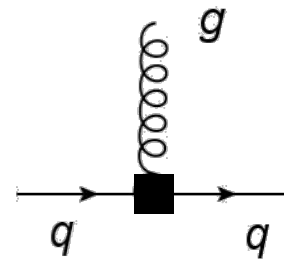
$$\begin{aligned}
 \mathcal{L}_{PT} = & -\bar{\theta} \frac{g^2}{64\pi^2} \epsilon^{\mu\nu\alpha\beta} G_{\mu\nu}^a G_{\alpha\beta}^a - \frac{1}{2} \sum_{q=u,d} \left(d_q \bar{q} i \sigma^{\mu\nu} \gamma_5 q F_{\mu\nu} + \tilde{d}_q \bar{q} i \sigma^{\mu\nu} \gamma_5 t_a q G_{\mu\nu}^a \right) \\
 & + \frac{d_W}{6} f_{abc} \epsilon^{\mu\nu\alpha\beta} G_{\alpha\beta}^a G_{\mu\rho}^b G_{\nu\rho}^c + \sum_{i,j,k,l=u,d} C_{ijkl} \bar{q}_i \Gamma q_j \bar{q}_k \Gamma' q_l
 \end{aligned}$$

Next: nonperturbative QCD

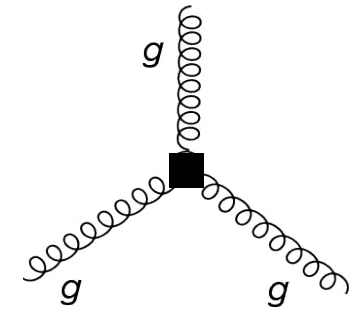
QCD θ -term



quark EDM



quark color-EDM

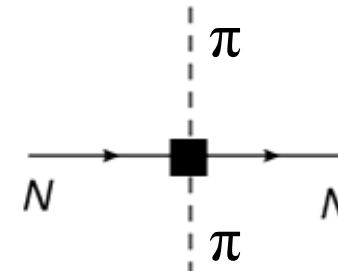
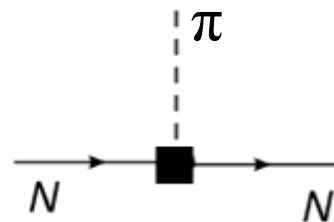


gluon color-EDM

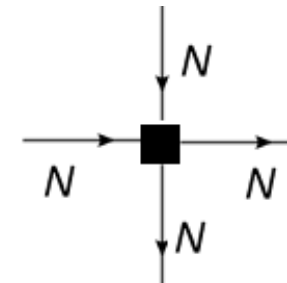
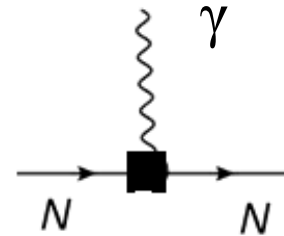
✓ 1 GeV

Q

χ PT = chiral
perturbation
theory

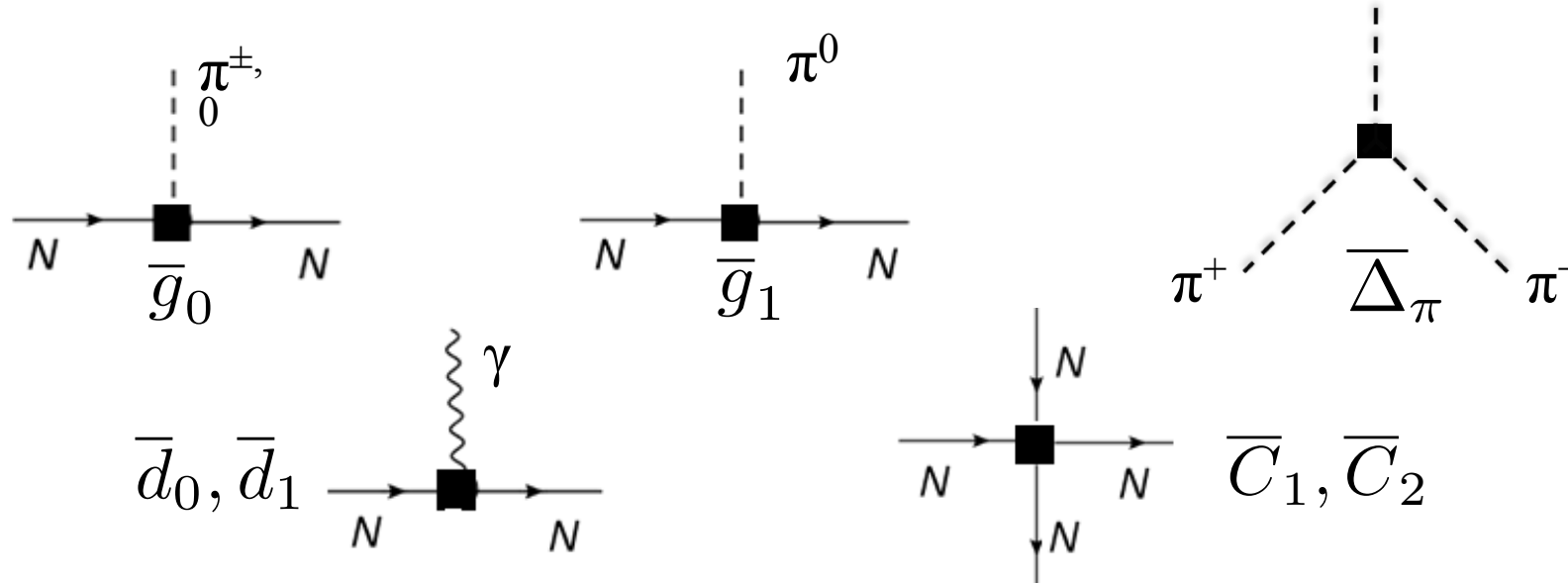


✓ 100 MeV



The magnificent seven

- ✓ T violation at nuclear scales (non-perturbative QCD) from



$$\mathcal{L} = -2\bar{N}(\bar{d}_0 + \bar{d}_1\tau_3)S^\mu N v^\nu F_{\mu\nu} + \bar{g}_0\bar{N}\vec{\tau} \cdot \vec{\pi}N + \bar{g}_1\bar{N}\pi_3N + \bar{C}_1\bar{N}N\partial_\mu(\bar{N}S^\mu N) + \bar{C}_2\bar{N}\vec{\tau}N \cdot \partial_\mu(\bar{N}S^\mu\vec{\tau}N)$$

- ✓ Different models of CP violation predict a different hierarchy!
 - QCD theta term, left-right symmetric models, SUSY, multi-Higgs, ...

Example: the QCD theta term

- ✓ Theta term = chiral pseudo-vector, same as quark mass difference
 - Link to isospin violation

$$-\bar{\theta} \frac{g^2}{64\pi^2} \epsilon^{\mu\nu\alpha\beta} G_{\mu\nu}^a G_{\alpha\beta}^a \longrightarrow \frac{m_u m_d}{m_u + m_d} \bar{\theta} \bar{q} i \gamma_5 q$$

- ✓ P- and T-odd pion-nucleon interactions
 - Traditionally expected to be dominant, since er = long range

$$\bar{g}_0^\theta = \frac{(M_n - M_p)^{\text{strong}} (1 - \varepsilon^2)}{F_\pi} \bar{\theta} = -0.018(7) \bar{\theta}$$

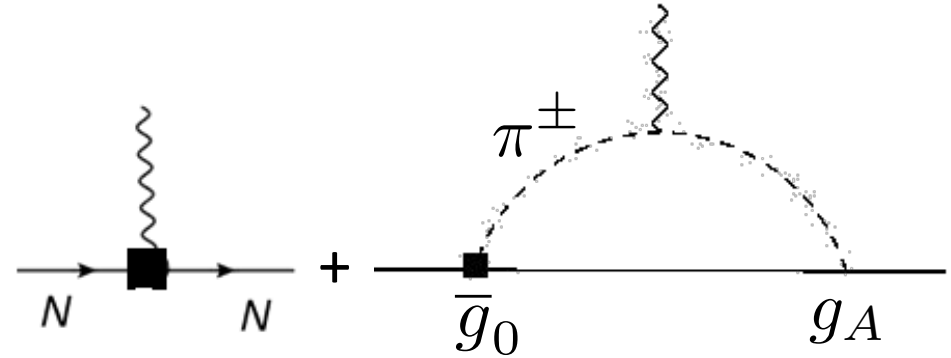
$$\bar{g}_1^\theta = \frac{8c_1 (\delta m_\pi^2)^{\text{strong}} (1 - \varepsilon^2)}{F_\pi} \bar{\theta} = 0.003(2) \bar{\theta}$$

- Input from phenomenology (πN σ -term) & LQCD

$$\varepsilon = \frac{m_u - m_d}{m_u + m_d} = -0.35(10)$$

Nucleon EDMs

- ✓ 1-loop diagrams UV divergent
 - 2 counterterms needed



$$d_n = \bar{d}_0 - \bar{d}_1 - \frac{eg_A\bar{g}_0}{4\pi^2 F_\pi} \left(\ln \frac{m_\pi^2}{M_N^2} - \frac{\pi m_\pi}{2 M_N} \right)$$

$$d_p = \bar{d}_0 + \bar{d}_1 + \frac{eg_A}{4\pi^2 F_\pi} \left[\bar{g}_0 \left(\ln \frac{m_\pi^2}{M_N^2} - 2\pi \frac{m_\pi}{M_N} \right) - \bar{g}_1 \frac{\pi m_\pi}{2 M_N} \right]$$

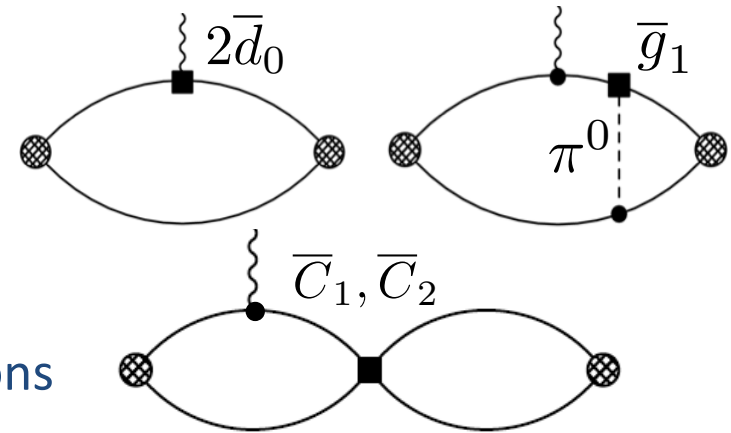
- 3 unknowns... can be fitted by any source
- For each source neutron & proton EDMs of same order
- Absorb loop contributions in $\bar{d}_{0,1}$

- ✓ For theta term, with LQCD input:
 - $d_n^\theta = -2.9(9) \times 10^{-16} \bar{\theta} \text{ e cm}$
 - $d_p^\theta = +1.1(1.1) \times 10^{-16} \bar{\theta} \text{ e cm}$

Deuteron EDM

✓ Contributions:

- Sum of nucleon EDMs = $d_n + d_p$
- T-violating pion exchange & NN interactions



✓ “Chiral filter”: deuteron is special case due to $N = Z$

- $^3S_1 \rightarrow ^3P_1$ with \bar{g}_1 coupling, back via E1 transition
- $^3S_1 \rightarrow ^1P_1$ with \bar{g}_0 coupling, no E1 back (same for \bar{C}_1, \bar{C}_2)

✓ Little model dependence

$$d_D = d_n + d_p + [0.180(23)\bar{g}_1 + 0.0028(3)\bar{g}_0] e \text{ fm}$$

- For quark color-EDM d_D is significantly larger than $d_n + d_p$

✓ Way to extract theta, or more generally \bar{g}_1 , from data

$$d_D^\theta = [-1.8(1.4) + 0.55(36)(5) - 0.05(2)(1)] \times 10^{-16} \bar{\theta} e \text{ cm}$$

Helion & triton EDMs

- ✓ Calculated for all sources in consistent EFT framework
 - Hadronic uncertainties still dominate over nuclear ones
 - Unreliable but small contributions from interactions with $\overline{C}_1, \overline{C}_2$

- ✓ For *e.g.* QCD theta term

$$d_{^3\text{He}}^{\overline{\theta}} = [-2.60(0.80) - 1.36(88)] \times 10^{-16} \overline{\theta} \text{ e cm}$$

$$d_{^3\text{H}}^{\overline{\theta}} = [+1.10(0.96) + 2.16(85)] \times 10^{-16} \overline{\theta} \text{ e cm}$$

- ✓ Master table:

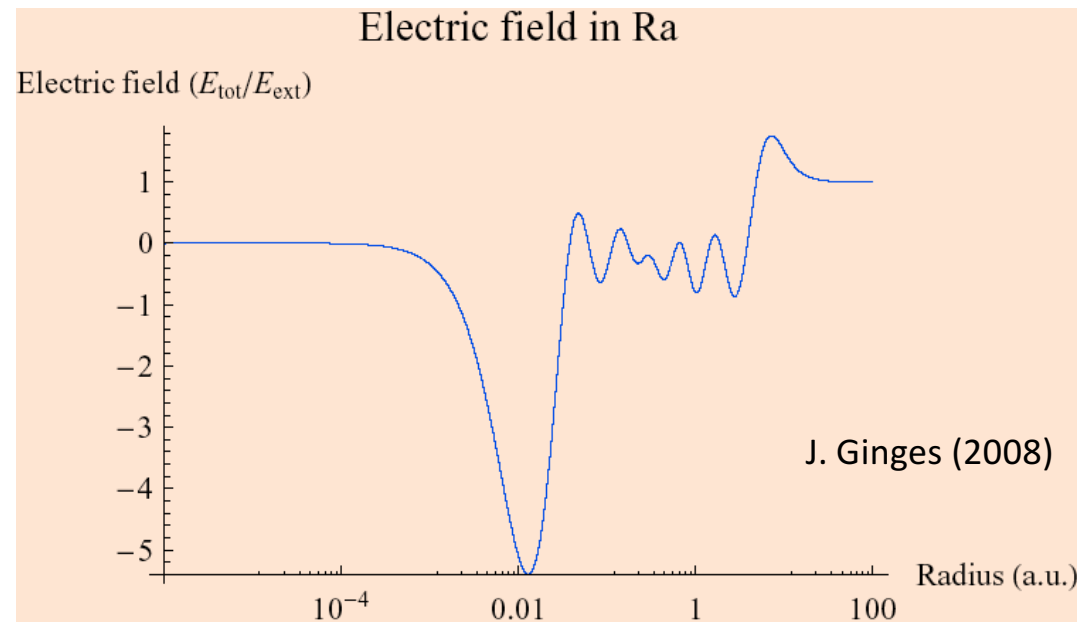
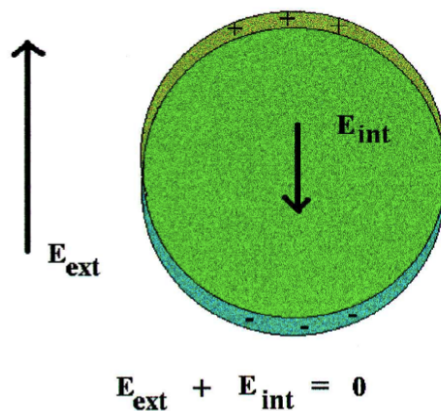
	d_0	d_1	g_0	g_1	C_1	C_2
n	1	-1	-	-	-	-
p	1	1	-	-	-	-
D	2	0	≈ 0	-0.19	-	-
^3He	0.83	-0.93	-0.15	-0.28	-0.01	0.02
^3H	0.85	0.95	0.15	-0.28	0.01	-0.02

- Clear strategy to disentangle the sources!

The Schiff shielding theorem

- ✓ EDM of a nonrelativistic atom = 0 *i.e.* point particles, Coulomb force
 - Electrostatic force balance, rearrangement of constituents
- ✓ Loopholes for measurability of EDMs (Schiff, 1963; Sandars, 1965)
 - Relativistic (e) + finite-size (N) + magnetic (e - N) effects
 - Residual interaction = P- and T-odd *Schiff moment*

- ✓ The theorem at work:



EDMs of diamagnetic atoms

PRL 116, 161601 (2016)

PHYSICAL REVIEW LETTERS

week ending
22 APRIL 2016



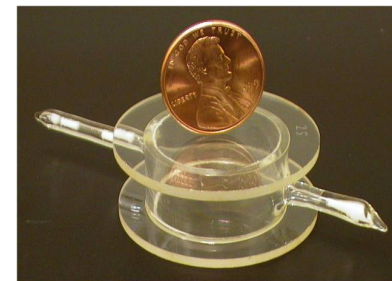
Reduced Limit on the Permanent Electric Dipole Moment of ^{199}Hg

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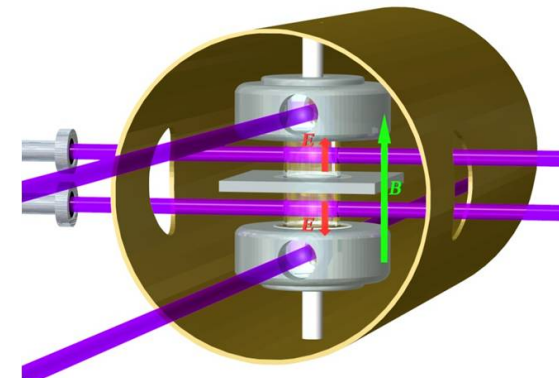
(Received 19 January 2016; revised manuscript received 8 March 2016; published 18 April 2016)

This Letter describes the results of the most recent measurement of the permanent electric dipole moment (EDM) of neutral ^{199}Hg atoms. Fused silica vapor cells containing enriched ^{199}Hg are arranged in a stack in a common magnetic field. Optical pumping is used to spin polarize the atoms orthogonal to the applied magnetic field, and the Faraday rotation of near-resonant light is observed to determine an electric-field-induced perturbation to the Larmor precession frequency. Our results for this frequency shift are consistent with zero; we find the corresponding ^{199}Hg EDM $d_{\text{Hg}} = (-2.20 \pm 2.75_{\text{stat}} \pm 1.48_{\text{syst}}) \times 10^{-30} e \text{ cm}$. We use this result to place a new upper limit on the ^{199}Hg EDM $|d_{\text{Hg}}| < 7.4 \times 10^{-30} e \text{ cm}$ (95% C.L.), improving our previous limit by a factor of 4. We also discuss the implications of this result for various CP -violating observables as they relate to theories of physics beyond the standard model.



✓ Nuclear EDM shielded

- Suppression factor $4Z^2 R_N/a_0 \approx 3 \times 10^{-4}$
- Hypersensitive experiments possible
- Difficult to interpret theoretically



✓ ^{225}Ra : octupole deformation \rightarrow factor 10-100 enhancement

✓ ^{129}Xe : co-located with ^3He + SQUIDs \rightarrow superlong spin coherence time

EDM of the ^{199}Hg atom

- ✓ Atomic part reasonably under control $d_{\text{Hg}} = 2.8(6) \times 10^{-4} S_{\text{Hg}} \text{ fm}^{-2}$
- ✓ Nuclear part not... $S_{\text{Hg}} = [0.4(3)\bar{g}_0 + 0.4(8)\bar{g}_1] e \text{ fm}^3$
 - Complicated many-body calculation with a nuclear model

Group	Method	a_0	a_1	a_2
Flambaum <i>et al.</i>	Schematic	0.087	0.087	0.174
Dmitriev, Sen'kov	Phen. RPA	0.00004	0.055	0.009
de Jesus, Engel	Skyrme QRPA	0.002-0.010	0.057-0.090	0.011-0.025
Engel <i>et al.</i>	Odd-A Skyrme MF	0.009-0.041	-0.027-+0.005	0.009-0.024

- Core polarization is important, quenches single-particle result
 - Contribution from nucleon EDMs?
 - Reasons for discrepancies not clear... ^{199}Hg = difficult, “soft” nucleus
- ✓ At present could not be used to extract *e.g.* the value of θ_{QCD} ...

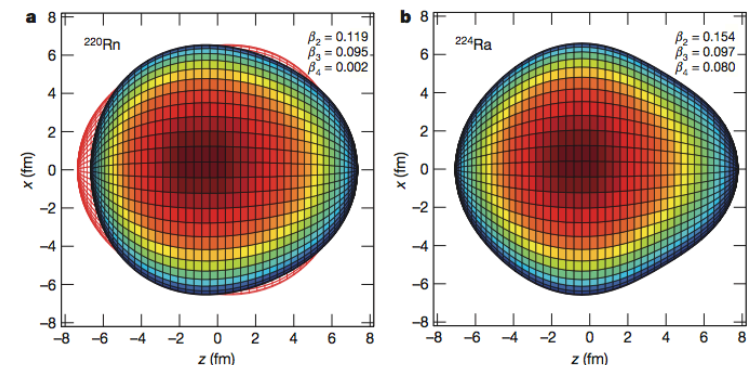
EDM of the ^{225}Ra atom

- ✓ Big enhancement from atomic degeneracy
- ✓ Additional factor $O(5 \times 10^{1-2})$ from octupole (“pear-shaped”) deformation
 - Shape asymmetry leads to parity doubling
 - ^{225}Ra : low-lying excited $1/2^-$ state 55 keV above $1/2^+$ ground state
 - Calculations claimed to be more reliable than for ^{199}Hg

Group	Method	a_0	a_1	a_2
Spevak <i>et al.</i>	Octupole-def. WS	-18.6	18.6	-37.2
Dobaczewski, Engel	Odd-A Skyrme MF	-1.0-(-4.7)	6.0-21.5	-3.9-(-11.0)

- ✓ Schiff moment correlated with E3 transitions
 - Measured @ ISOLDE in ^{220}Rn , ^{224}Ra
- ✓ 2016: First limit on ^{225}Ra EDM

Gaffney *et al.* (2013)



Comparison

Nucleus	Method	a_0	a_1	a_2
^{129}Xe	Phen. RPA	-0.0008	-0.0006	-0.0009
^{199}Hg	Several	0.01	± 0.02	0.02
^{225}Ra	Odd-A Skyrme MF	-1.5	6.0	-4.0

- ✓ ^{129}Xe factor 10 less sensitive as ^{199}Hg , also “difficult” nucleus
- ✓ Enhancements in ^{225}Ra overcome the Schiff screening
 - Similar sensitivity as light nuclei
- ✓ Job of nuclear-structure calculations: $S = S(d_n, d_p, \bar{g}_0, \bar{g}_1, \bar{C}_1, \bar{C}_2, \bar{\Delta}_\pi)$
 - Requires a chiral EFT for heavy nuclei
 - Microscopic nuclear calculations using few-nucleon input
 - Careful implementation of the Schiff theorem

Amplification of eEDMs in paramagnetic atoms

- ✓ Shielding factor (Sandars, 1965) $K_{\text{atom}} = d_{\text{atom}}/d_e \simeq Z^3 \alpha^2 \chi$
 - $Z^2 \alpha^2$ is relativistic factor, Z from E -field of nucleus
 - χ is polarizability, ≈ 10 for Cs

$$\mathbf{d}_{\text{atom}} = \sum_{n'} \frac{\langle ns | -d_e(\beta - 1)\boldsymbol{\sigma} \cdot \mathbf{E} | n'p \rangle \langle n'p | -e\mathbf{r} | ns \rangle}{E_{ns} - E_{n'p}} + c.c.$$

- ✓ Requires an atomic-structure calculation for $_{37}\text{Rb}$, $_{55}\text{Cs}$, $_{81}\text{Tl}$, $_{87}\text{Fr}$, $_{88}\text{Ra}^*$
 - $d_{\text{atom}}/d_e \approx 24, 114, -570, 1150, 40.000$ for calculations

$$K_{\text{Tl}} = -(570 \pm 20) \rightarrow d_e < 1.6 \times 10^{-27} \text{ ecm}$$

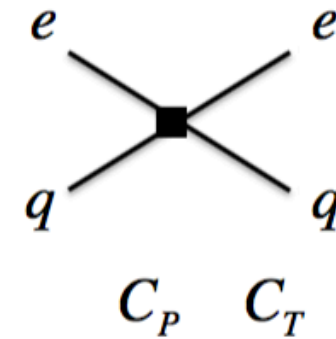
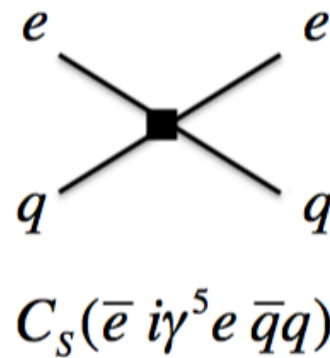
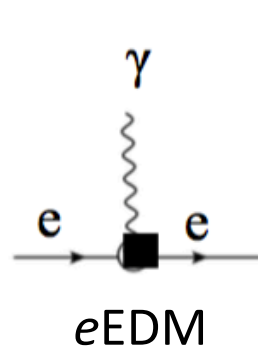
- *Caveat: T-odd electron-nucleon forces!*

$$d_{\text{Tl}} = -(570 \pm 20)d_e - (7.0 \pm 2.0) \times 10^{-18} C_S \text{ ecm}$$

(Semi-)leptonic CP violation

✓ Four operators @ 1 GeV

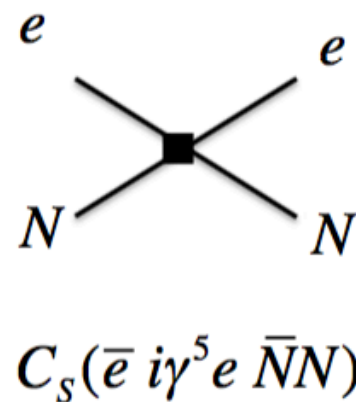
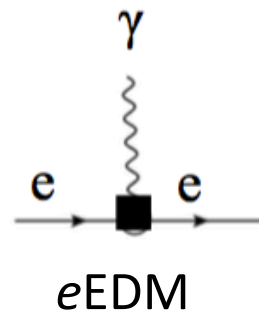
✓ 1 GeV



Focus on these two

Usually left out

✓ 0.1 GeV

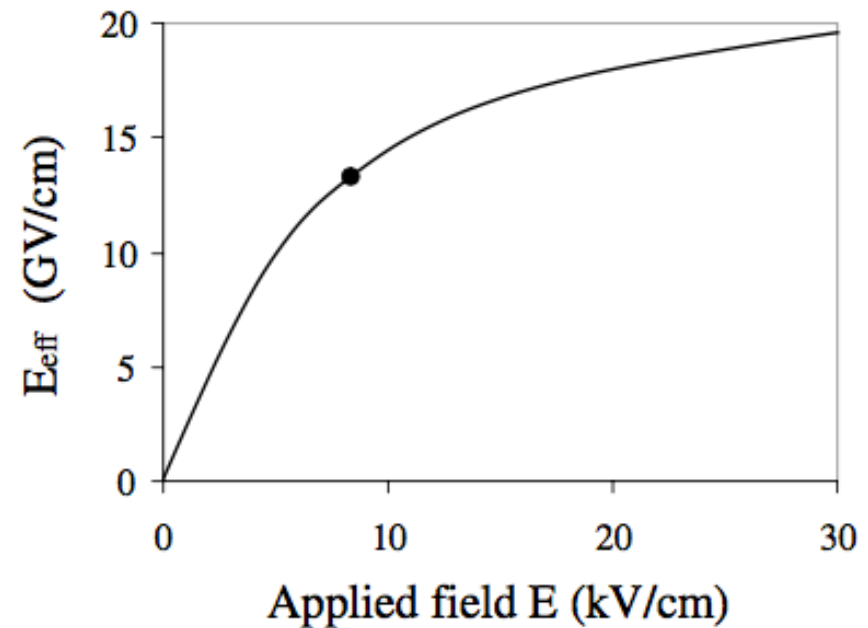
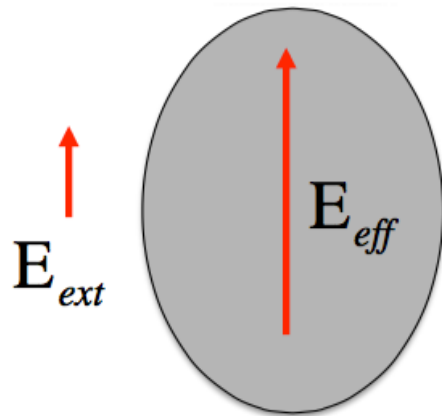


Hadronic matrix elements relatively well-known

Polar molecules

- ✓ Convert strong external electric field to HUGE internal field
 - Effective field = nonlinear function of external field

$$\Delta E \simeq E_{eff}(E_{ext}) d_e$$



- From J. Hudson *et al.*, PRL 2002

$$\Delta E_{YbF} = (15 \pm 2) \text{ GeV} \left[\frac{d_e}{e_{cm}} \right] + \mathcal{O}(C_S)$$

$$\Delta E_{ThO} = (80 \pm 10) \text{ GeV} \left[\frac{d_e}{e_{cm}} \right] + \mathcal{O}(C_S)$$

Polar molecules

- ✓ Assume no cancellation with C_S
 - OR no cancellation with eEDM

- ✓ Find a signal, what is responsible?
 - Strong correlations
 - Need two measurements

	Tl	YbF	ThO
β/α in $10^{-20} e.cm$	1.15	0.85	1.25

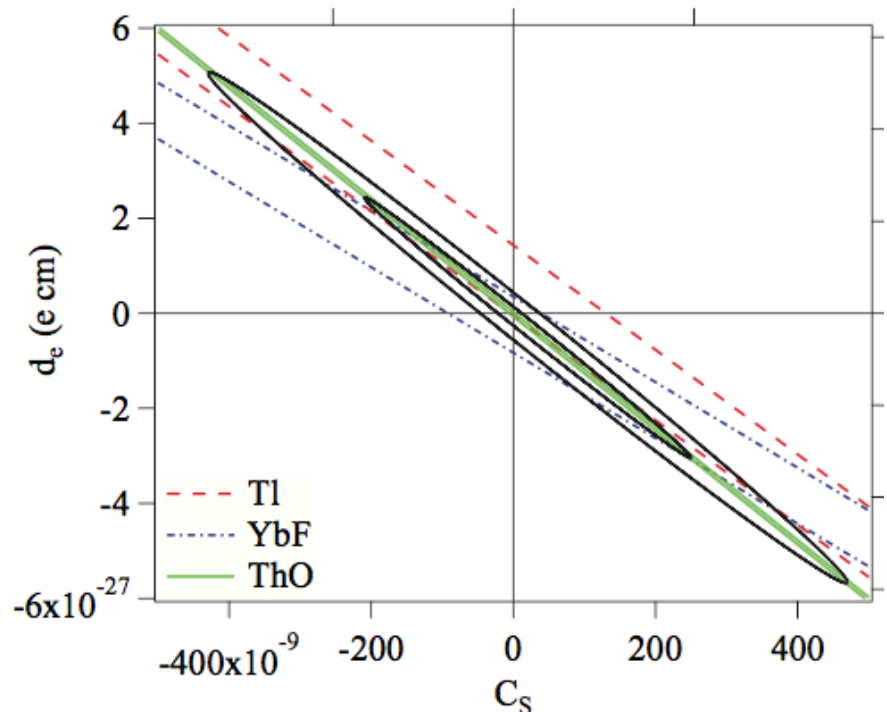
- ✓ Pseudo-scalar & tensor interactions?
 - Constraints from para- (Cs, Fr)
 - or diamagnetic atoms (Xe, Hg, Ra)?

- ✓ Several models have one dominant source, e.g. eEDM in mLRSM

$$d_e < 8.7 \times 10^{-29} \text{ ecm}$$

$$C_S < 5.9 \times 10^{-9}$$

$$\Delta E = \alpha d_e + \beta C_S$$

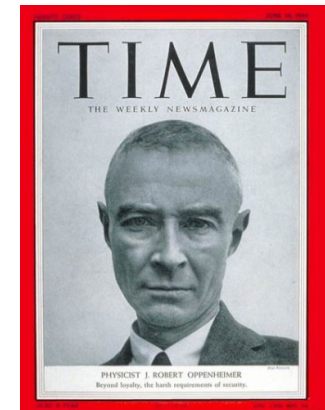
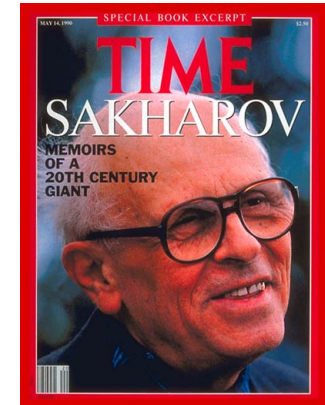


A historical curiosity @ Brussels

- ✓ Matter-antimatter asymmetry of the Universe requires (1967)
 - Violation of baryon number
 - Violation of C and CP
 - Departure of thermal equilibrium
 - (or: CPT violation)

- ✓ Not enough CP violation within the SM, off by factor $O(10^9)$
 - Physics at a new scale of $O(\text{TeV}) \rightarrow$ measurable EDMs?
 - *Caveat*: Leptogenesis!

- ✓ *“If the weak interactions of atomic physics would – contrary to expectation – not be invariant for time inversion, would this have any consequences for cosmological or cosmogonic questions?”*
 - J. R. Oppenheimer after talk “The arrow of time” by T. Gold
 - “La structure et l’évolution de l’Univers”, Onzième conseil de physique, Bruxelles, 9-13 juin 1958



Take-home messages

- ✓ Message 1: EDM experiments are HYPER-sensitive
 - Next generation probes energy scales up to 10 - 100 TeV

- ✓ Message 2: EDMs are ULTRA-relevant to SUPER-symmetry *et al.*
 - Upon discovery, we can disentangle the sources of CP violation

- ✓ *“Data! Data! Data! We cannot make bricks without clay!”*
 - *“It is quite a three-pipe problem...”*

